# **Solving Two-Step Inequalities**

**Essential Question** How can you use an inequality to describe the dimensions of a figure?

# **ACTIVITY:** Areas and Perimeters of Figures

Work with a partner.

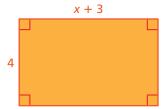
- Use the given condition to choose the inequality that you can use to find the possible values of the variable. Justify your answer.
- Write four values of the variable that satisfy the inequality you chose.
- **a.** You want to find the values of *x* so that the area of the rectangle is more than 22 square units.

$$4x + 12 > 22$$

$$4x + 3 > 22$$

$$4x + 12 \ge 22$$

$$2x + 14 > 22$$



**b.** You want to find the values of x so that the perimeter of the rectangle is greater than or equal to 28 units.

$$x + 7 \ge 28$$

$$4x + 12 \ge 28$$

$$2x + 14 \ge 28$$

$$2x + 14 \le 28$$

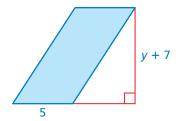
**c.** You want to find the values of *y* so that the area of the parallelogram is fewer than 41 square units.

$$5y + 7 < 41$$

$$5y + 35 < 41$$

$$5y + 7 \le 41$$

$$5y + 35 \le 41$$



10

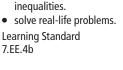
**d.** You want to find the values of z so that the area of the trapezoid is at most 100 square units.

$$5z + 30 \le 100$$

$$10z + 30 \le 100$$

$$5z + 30 < 100$$

$$10z + 30 < 100$$



COMMON CORE

**Inequalities** In this lesson, you will solve multi-step

7.EE.4b

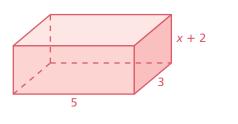
## ACTIVITY: Volumes of Rectangular Prisms

Work with a partner.

Math

State the
Meaning of
Symbols
What inequality
symbols do the
phrases at least
and no more than
represent? Explain.

- Use the given condition to choose the inequality that you can use to find the possible values of the variable. Justify your answer.
- Write four values of the variable that satisfy the inequality you chose.
- **a.** You want to find the values of *x* so that the volume of the rectangular prism is at least 50 cubic units.



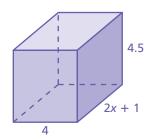
$$15x + 30 > 50$$

$$x + 10 \ge 50$$

 $15x + 30 \ge 50$ 

 $15x + 2 \ge 50$ 

**b.** You want to find the values of *x* so that the volume of the rectangular prism is no more than 36 cubic units.



$$8x + 4 < 36$$

$$36x + 18 < 36$$

$$2x + 9.5 \le 36$$

 $36x + 18 \le 36$ 

# What Is Your Answer?

- **3. IN YOUR OWN WORDS** How can you use an inequality to describe the dimensions of a figure?
- **4.** Use what you know about solving equations and inequalities to describe how you can solve a two-step inequality. Give an example to support your explanation.



Use what you learned about solving two-step inequalities to complete Exercises 3 and 4 on page 150.



You can solve two-step inequalities in the same way you solve two-step equations.

### **EXAMPLE**

#### Solving Two-Step Inequalities

a. Solve  $5x - 4 \ge 11$ . Graph the solution.

$$5x - 4 \ge 11$$

Write the inequality.



Addition Property of Inequality

$$5x \ge 15$$

Simplify.

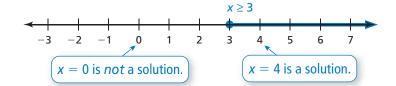
Step 2: Undo the multiplication. 
$$\frac{5x}{5} \ge \frac{15}{5}$$

**Division Property of Inequality** 

$$x \ge 3$$

Simplify.

The solution is  $x \ge 3$ .



b. Solve  $\frac{b}{-3}$  + 4 < 13. Graph the solution.

$$\frac{b}{-3} + 4 < 13$$

Write the inequality.

Step 1: Undo the addition. 
$$\longrightarrow -4 -4$$

**Subtraction Property of Inequality** 

$$\frac{b}{-3}$$
 < 9

Simplify.

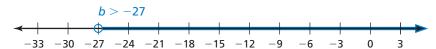
Step 2: Undo the division. 
$$\longrightarrow$$
  $-3 \cdot \frac{b}{-3} > -3 \cdot 9$ 

Use the Multiplication Property of Inequality. Reverse the inequality symbol.

$$b > -27$$

Simplify.

The solution is b > -27.



#### On Your Own

Now You're Ready Exercises 5-10

Solve the inequality. Graph the solution.

1. 
$$6y - 7 > 5$$

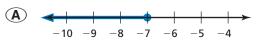
**2.** 
$$4 - 3d \ge 19$$

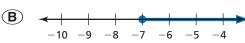
**1.** 
$$6y - 7 > 5$$
 **2.**  $4 - 3d \ge 19$  **3.**  $\frac{w}{-4} + 8 > 9$ 

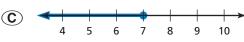
### **EXAMPLE**

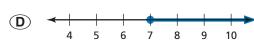
### **Graphing an Inequality**

Which graph represents the solution of  $-7(x+3) \le 28$ ?









$$-7(x+3) \le 28$$

$$-7x - 21 \le 28$$

**Distributive Property** 

Step 1: Undo the subtraction. 
$$+21 + 21 -7x \le 49$$

Addition Property of Inequality

Step 2: Undo the multiplication. 
$$\rightarrow \frac{-7x}{-7} \ge \frac{49}{-7}$$

Simplify.

Use the Division Property of Inequality. Reverse the inequality symbol.

 $x \ge -7$ 

Simplify.

The correct answer is  $(\mathbf{B})$ .

## **EXAMPLE**

## **Real-Life Application**

#### **Progress Report Month Pounds Lost** 1 12 2 9 3 5 4 8

A contestant in a weight-loss competition wants to lose an average of at least 8 pounds per month during a 5-month period. How many pounds must the contestant lose in the fifth month to meet the goal?

Write and solve an inequality. Let x be the number of pounds lost in the fifth month.

$$\frac{12 + 9 + 5 + 8 + x}{5} \ge 8$$

$$\frac{34 + x}{5} \ge 8$$

The phrase at least means greater than or equal to.

$$\frac{34+x}{5} \ge 8$$

Simplify.

$$5 \cdot \frac{34 + x}{5} \ge 5 \cdot 8$$

**Multiplication Property of Inequality** 

$$34 + x \ge 40$$

Simplify.

$$x \ge 6$$

Subtract 34 from each side.

# In Example 3, the

Remember

average is equal to the sum of the pounds lost divided by the number of months.

So, the contestant must lose at least 6 pounds to meet the goal.



Now You're Ready Exercises 12-17

Solve the inequality. Graph the solution.

**4.** 
$$2(k-5) < 6$$

**5.** 
$$-4(n-10) < 32$$
 **6.**  $-3 \le 0.5(8+y)$ 

**6.** 
$$-3 \le 0.5(8 + \nu)$$

7. WHAT IF? In Example 3, the contestant wants to lose an average of at least 9 pounds per month. How many pounds must the contestant lose in the fifth month to meet the goal?

#### 4.4 Exercises





# Vocabulary and Concept Check

- 1. WRITING Compare and contrast solving two-step inequalities and solving two-step equations.
- **2. OPEN-ENDED** Describe how to solve the inequality 3(a + 5) < 9.



# Practice and Problem Solving

Match the inequality with its graph.

3. 
$$\frac{t}{3} - 1 \ge -3$$





Solve the inequality. Graph the solution.

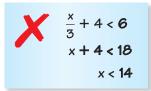
- **5.** 8y 5 < 3

- **6.**  $3p + 2 \ge -10$
- 7.  $2 > 8 \frac{4}{3}h$

**8.**  $-2 > \frac{m}{6} - 7$ 

- **9.**  $-1.2b 5.3 \ge 1.9$
- **10.**  $-1.3 \ge 2.9 0.6r$

11. ERROR ANALYSIS Describe and correct the error in solving the inequality.



Solve the inequality. Graph the solution.

- 2 **12.** 5(g+4) > 15
- **13.**  $4(w-6) \le -12$
- **14.**  $-8 \le \frac{2}{5}(k-2)$

- **15.**  $-\frac{1}{4}(d+1) < 2$
- **16.** 7.2 > 0.9(n + 8.6)
- **17.**  $20 \ge -3.2(c-4.3)$



**18. UNICYCLE** The first jump in a unicycle high-jump contest is shown. The bar is raised 2 centimeters after each jump. Solve the inequality  $2n + 10 \ge 26$  to find the number of additional jumps needed to meet or exceed the goal of clearing a height of 26 centimeters.

Solve the inequality. Graph the solution.

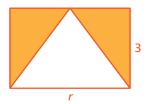
**19.** 
$$9x - 4x + 4 \ge 36 - 12$$

**20.** 
$$3d - 7d + 2.8 < 5.8 - 27$$

- 21. SCUBA DIVER A scuba diver is at an elevation of −38 feet. The diver starts moving at a rate of −12 feet per minute. Write and solve an inequality that represents how long it will take the diver to reach an elevation deeper than −200 feet.
- **22. KILLER WHALES** A killer whale has eaten 75 pounds of fish today. It needs to eat at least 140 pounds of fish each day.
  - **a.** A bucket holds 15 pounds of fish. Write and solve an inequality that represents how many more buckets of fish the whale needs to eat.
  - **b.** Should the whale eat *four* or *five* more buckets of fish? Explain.



- **23. REASONING** A student theater charges \$9.50 per ticket.
  - **a.** The theater has already sold 70 tickets. Write and solve an inequality that represents how many more tickets the theater needs to sell to earn at least \$1000.
  - **b.** The theater increases the ticket price by \$1. Without solving an inequality, describe how this affects the total number of tickets needed to earn at least \$1000.
- 24. For what values of *r* will the area of the shaded region be greater than or equal to 12 square units?





# Fair Game Review What you learned in previous grades & lessons

Find the missing values in the ratio table. Then write the equivalent ratios. (Skills Review Handbook)

25.

Flutes	7		28
Clarinets	4	12	

26.

Boys	6	3	
Girls	10		50

- **27. MULTIPLE CHOICE** What is the volume of the cube? *(Skills Review Handbook)*
- $\bigcirc$  16 ft<sup>3</sup>
- **©**  $24 \text{ ft}^3$
- **D**  $32 \text{ ft}^3$

